

# Mathematical modelling of transport of coal stockpiles by tsunami at Sines port



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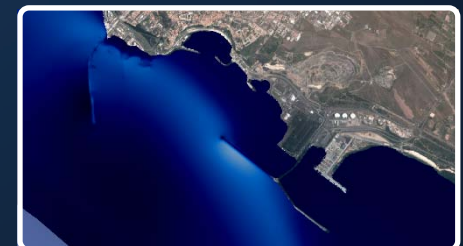
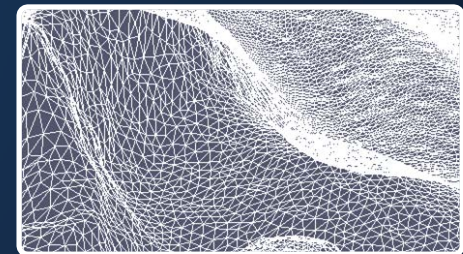
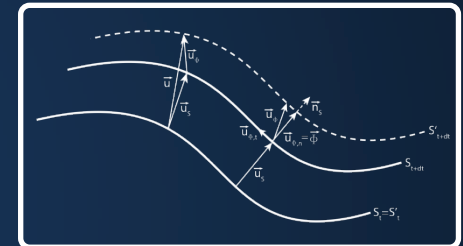
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- Lagrangian-Eulerian coupling
- Smoothed-Particle Hydrodynamics



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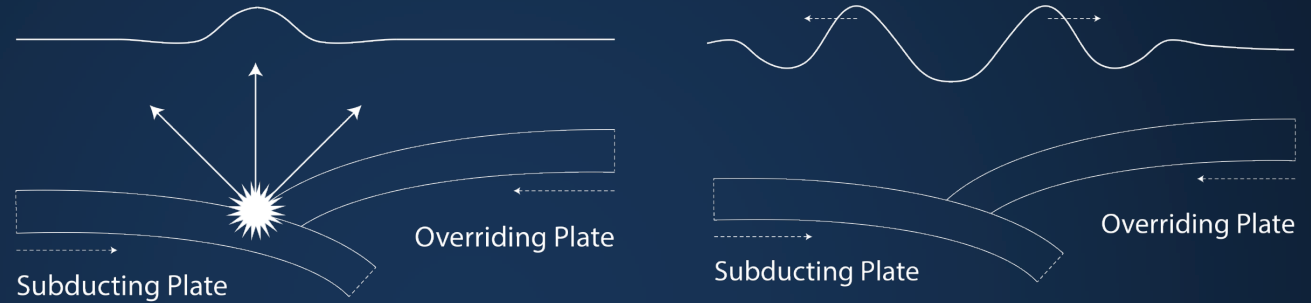
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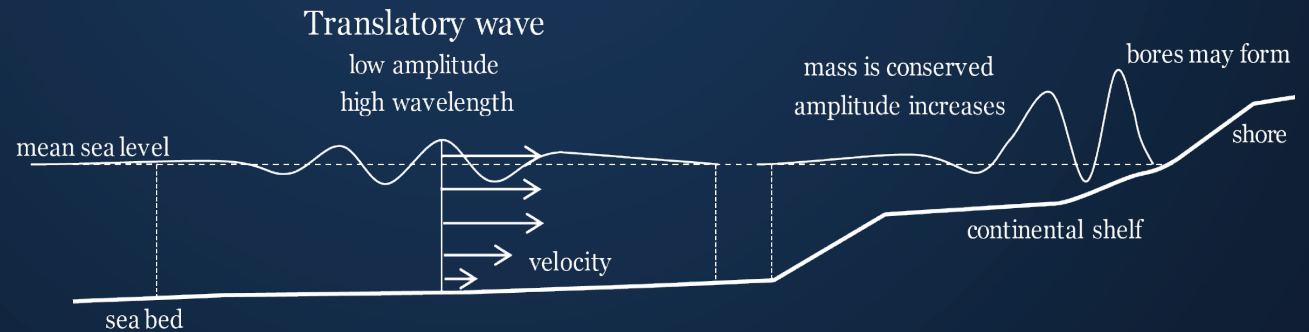
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# What is a tsunami?

## Generation mechanism



## Propagation and inundation



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# The Port of Sines

- **Open deep-sea port located in Sines, 150Km south of Lisbon.**
  - Began operating in 1978
  - 75 M€ investment over the last 10 years
  - Future plans for further expansion



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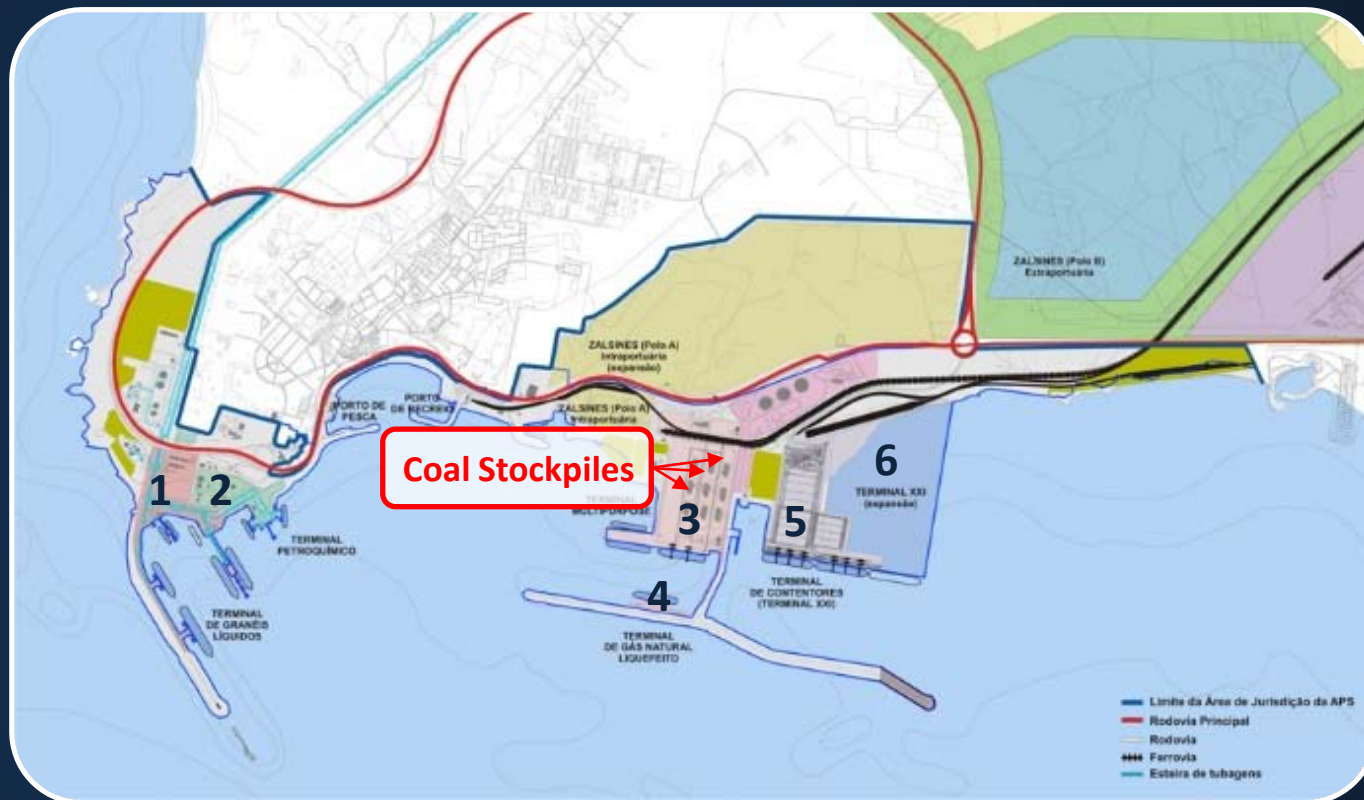
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# The Port of Sines



- 1 - Liquid Bulk Terminal
- 2 - Petrochemical Terminal
- 3 - Multipurpose Terminal

- 4 - Liquefied Natural Gas Terminal
- 5 - Container Terminal (Terminal XXI)
- 6 - Container Terminal Expansion

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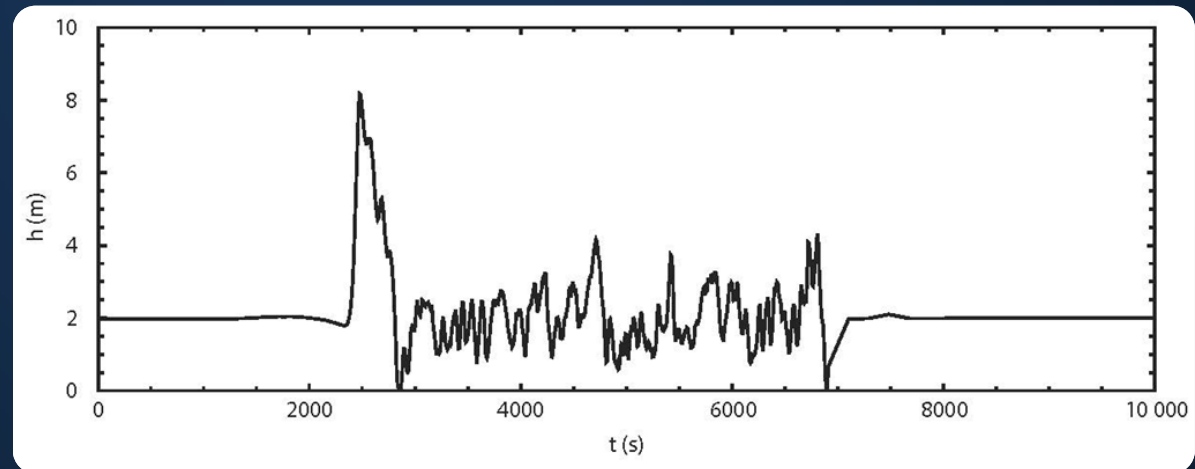
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# Initial and Boundary Conditions

- **High-tide scenario, approximately 2.0 m above mean sea level.**
- **Tsunami wave configuration similar to the one that struck Lisbon on the 1st November 1755.**
  - First wave measuring nearly 6 m above mean sea level



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# Mesh generation and refinement



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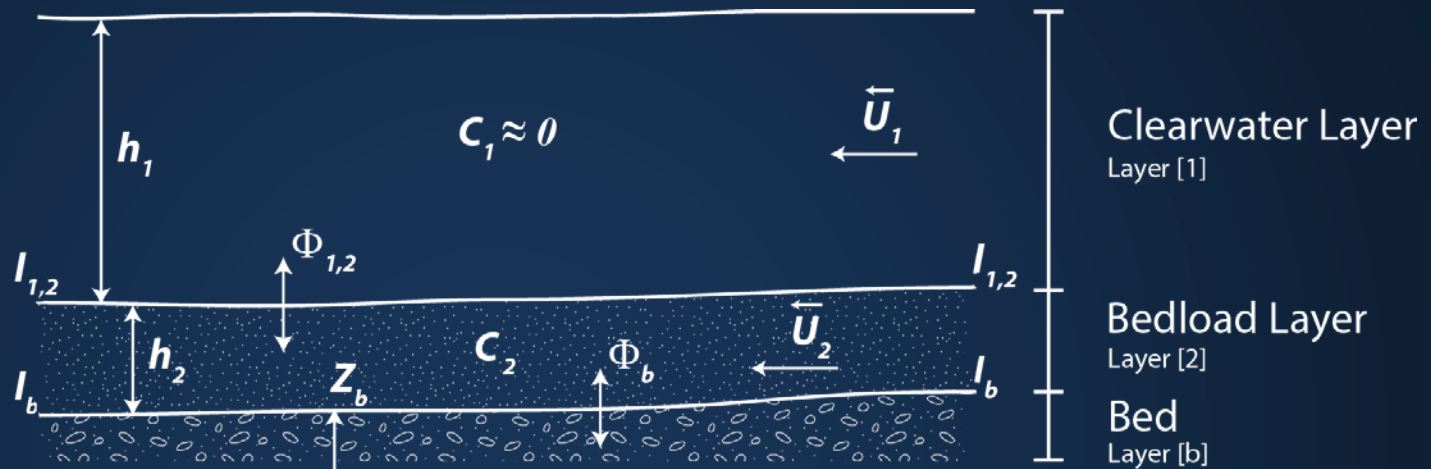
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# Conceptual Model



- **Clearwater Layer**
  - Negligible solid transport
- **Bedload Layer**
  - High concentration of solid material
  - Non-Newtonian rheological behavior

**References:** Ferreira (2005); Ferreira (2009); Canelas (2013) and Conde (2013)



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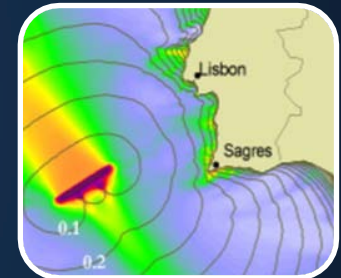
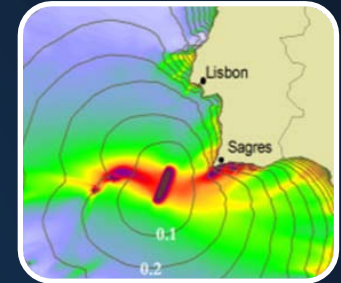
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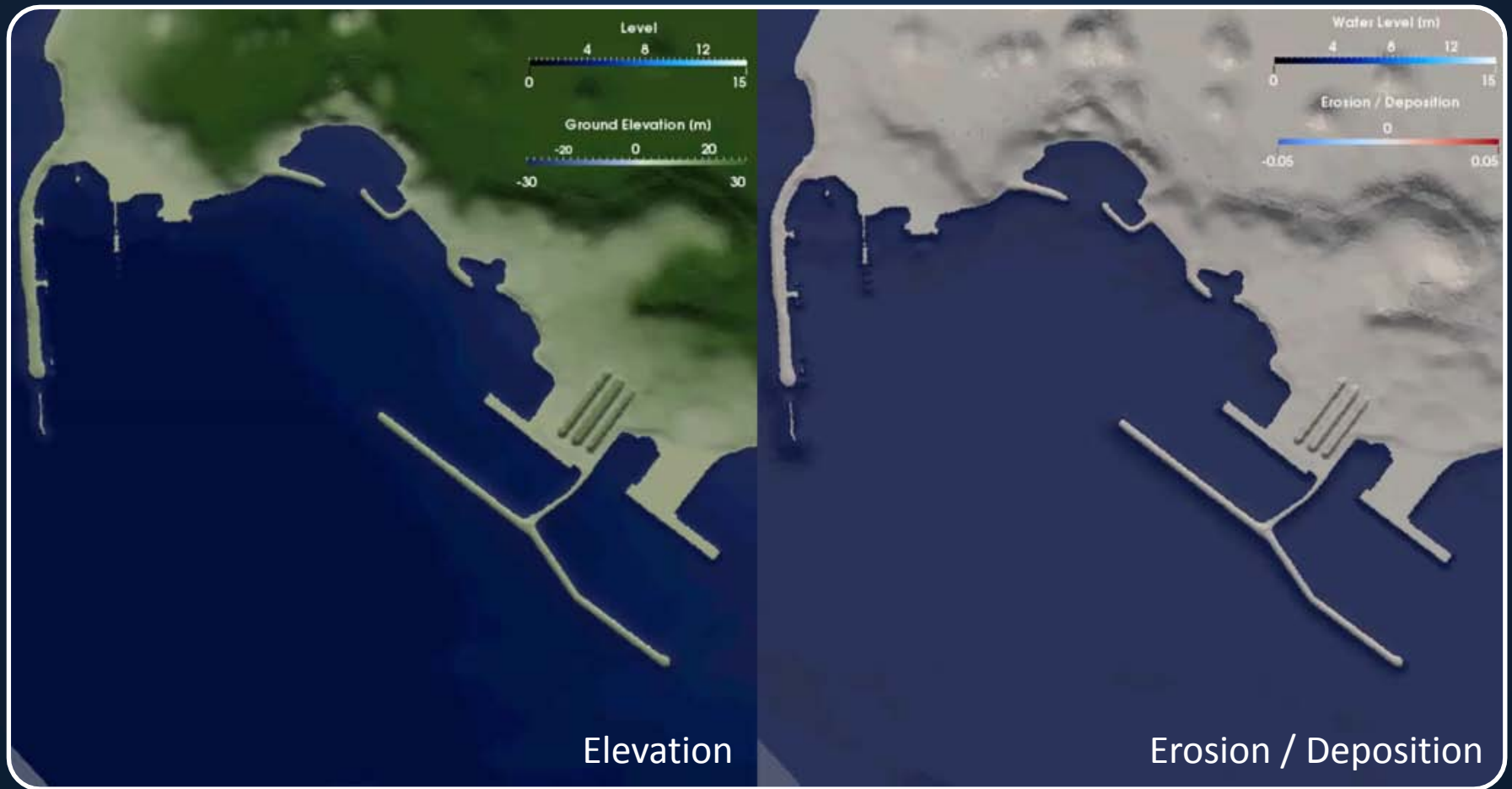
# Modelled scenarios

- **Tsunami propagating from Southwest**
  - Tsunami generated in the Marquês de Pombal fault.
  
- **Tsunami propagating from West**
  - Tsunami generated in the Gorringe bank.
  
- **Worst case scenario**
  - Tsunami generated in the Horseshoe and São Vicente faults.



# Tsunami propagating from Southwest (SW)

Possible tsunami source: Marquês de Pombal fault



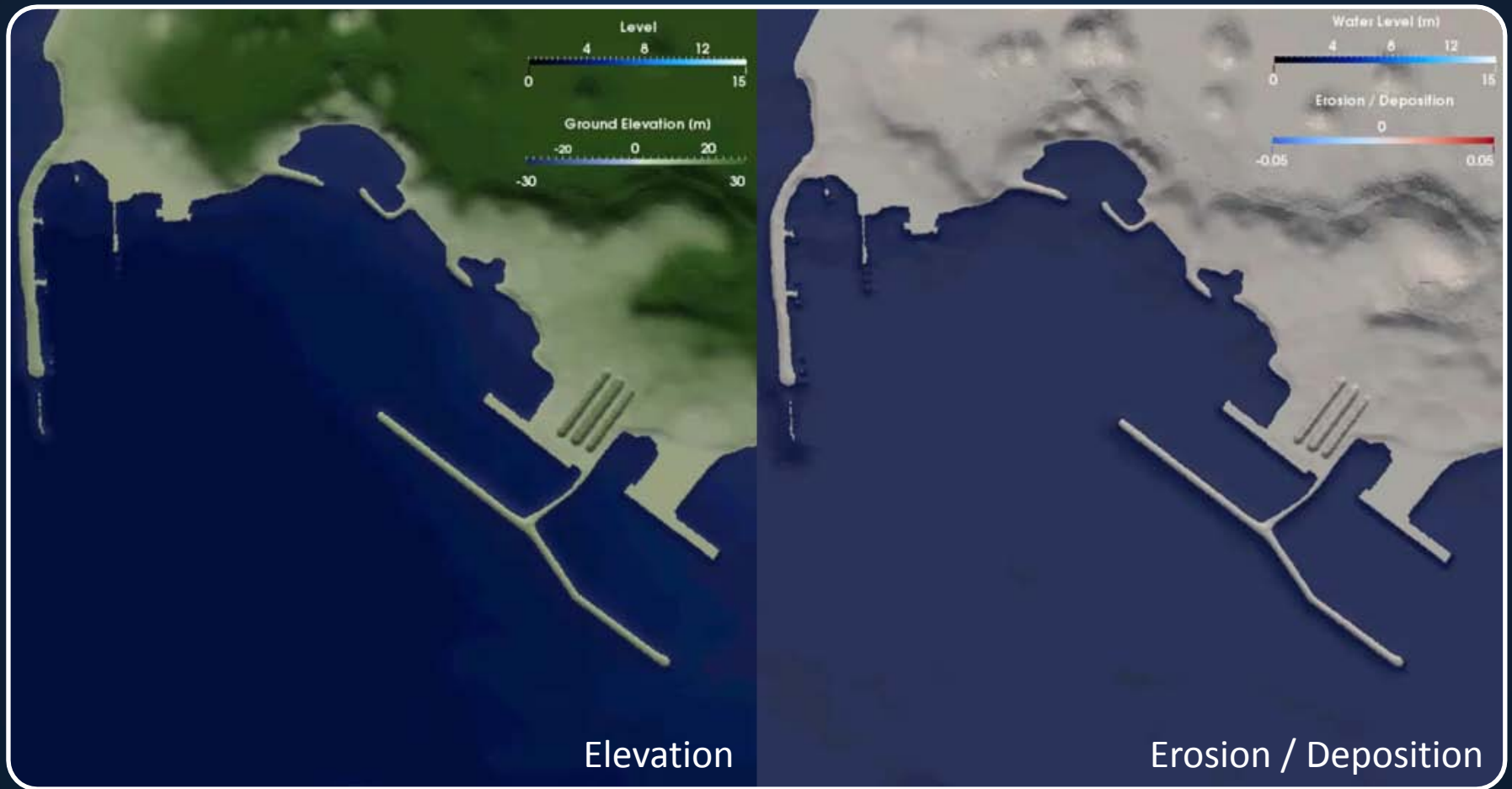
# Tsunami propagating from Southwest (SW)

Possible tsunami source: Marquês de Pombal fault



# Tsunami propagating from West (W)

Possible tsunami source: Gorringe bank fault



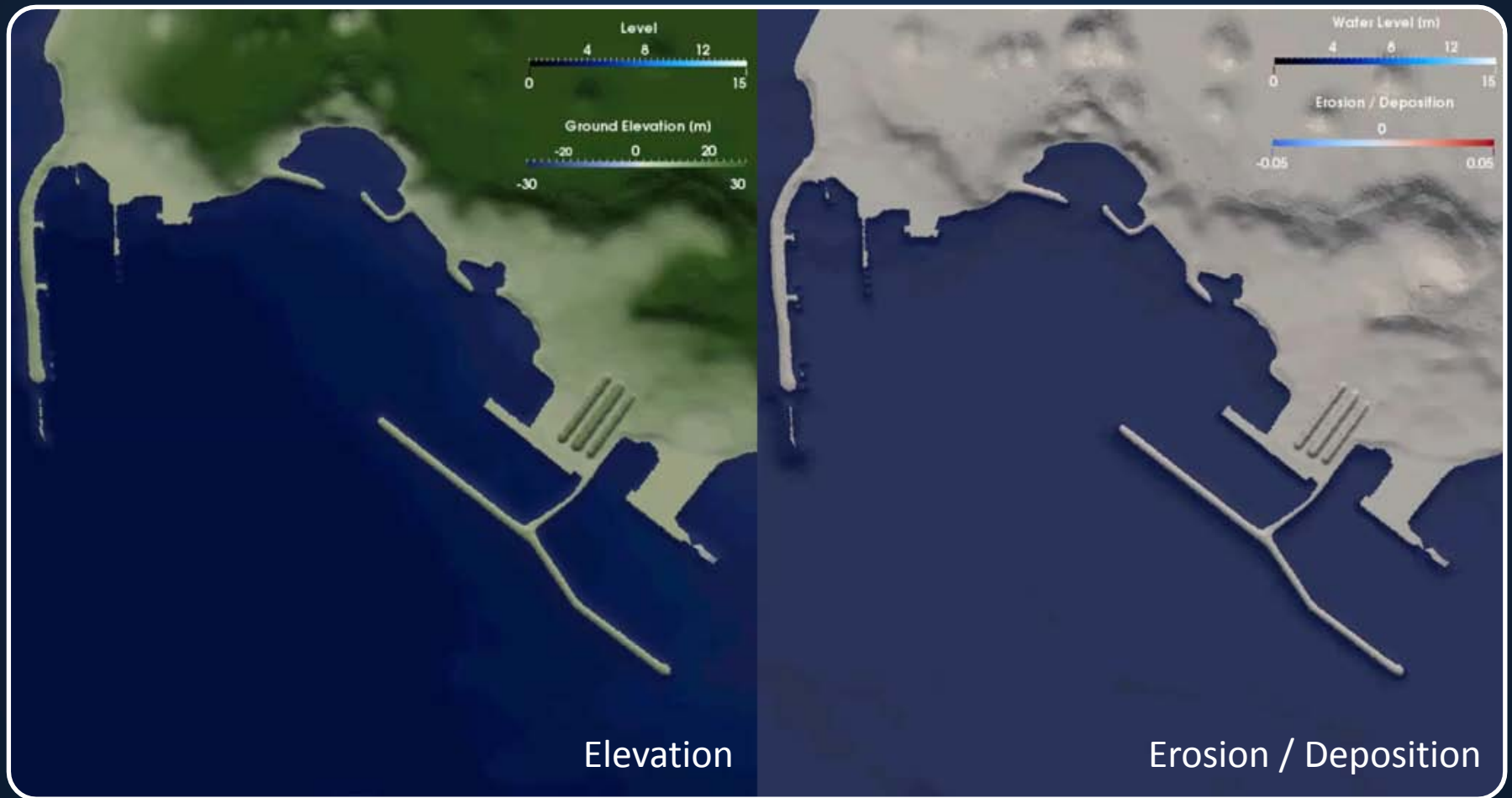
# Tsunami propagating from West (W)

Possible tsunami source: Gorringe bank fault



# Worst case scenario (SW and S)

Possible tsunami source: Combination of Horseshoe thrust fault and São Vicente fault



# Worst case scenario (SW and S)

Possible tsunami source: Combination of Horseshoe thrust fault and São Vicente fault



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# Conclusions

- **Regarding the inundation extent, all terminals are severely affected in all modelled scenarios.**
- **Coal is expected to be transported inland; this will cause economical losses and may cause negative environmental impacts.**
- **The drawdown stage will drive coal to the ocean, where it may be transported by oceanic currents (not modelled) or form underwater deposits.**



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# Future Developments

- **Lagrangian-Eulerian Coupling**  
Simulating container transport at Terminal XXI



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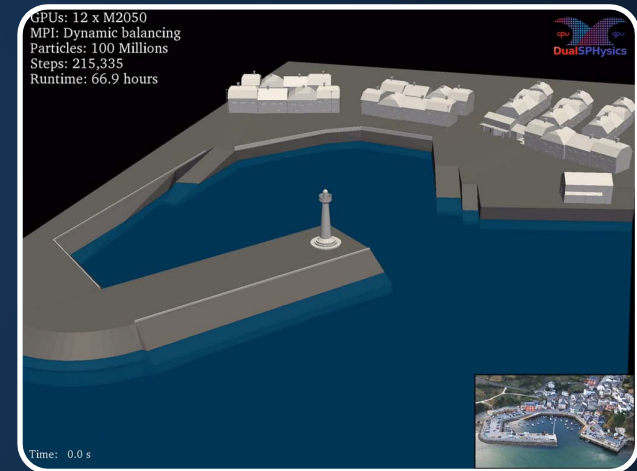
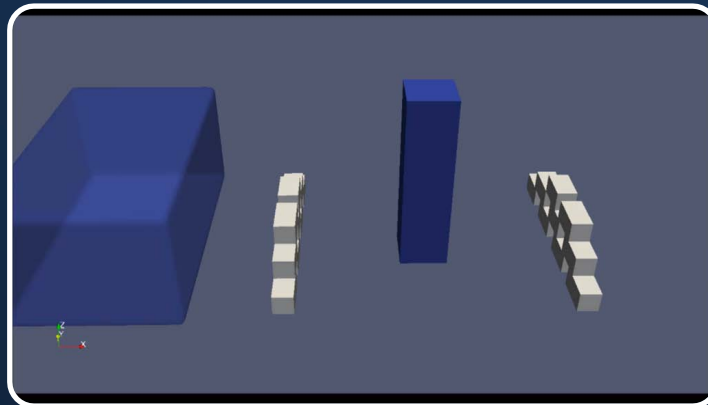
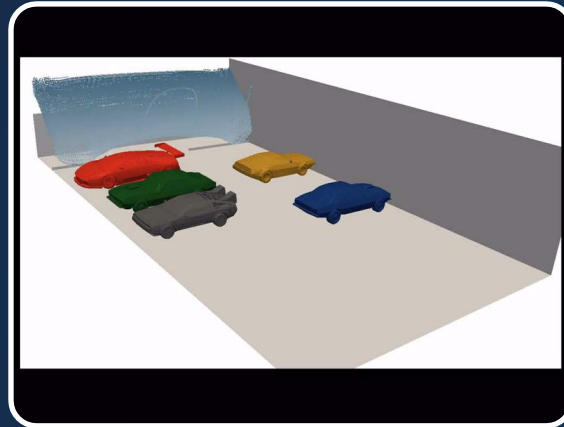
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# Future Developments

- **Smoothed-Particle Hydrodynamics with solid-fluid interactions**



# Thank you!

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## References:

Canelas, R., Murillo, J and Ferreira, R. M. L. (2013). Two dimensional depth averaged modelling of dam-break flows over mobile beds, *Journal of Hydraulics Research*, online first publication.

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# Conservation Laws

- **Conservation of total mass**

$$\frac{\partial}{\partial t}[\rho_L h_L] + \frac{\partial}{\partial x}[\rho_L U_L h_L] + \frac{\partial}{\partial y}[\rho_L V_L h_L] = \Phi_{L_u} \rho |_{z=L_u} - \Phi_{L_l} \rho |_{z=L_l}$$

- **Conservation of momentum**

$$\begin{aligned} \frac{\partial}{\partial t}[\rho_L U_{iL} h_L] + \frac{\partial}{\partial x_j}[\rho_L U_{iL} U_{jL} h_L] + \Phi_{L_l} [\rho u_i] |_{z=L_l} - \Phi_{L_u} [\rho u_i] |_{z=L_u} = \\ - \frac{\partial}{\partial x_i} P_L - \frac{\partial L_l}{\partial x_i} p |_{z=L_l} + \frac{\partial L_u}{\partial x_i} p |_{z=L_u} + \frac{\partial}{\partial x_j} T_{L_{ij}} h_L + \frac{\partial L_l}{\partial x_j} \tau_{ij} |_{z=L_l} - \frac{\partial L_u}{\partial x_j} \tau_{ij} |_{z=L_u} \end{aligned}$$

- **Conservation of bedload solid mass**

$$\frac{\partial}{\partial t}[C_L h_L] + \frac{\partial}{\partial x}[C_L U_L h_L] + \frac{\partial}{\partial y}[C_L V_L h_L] = C_L \Phi_{L_u} \frac{\rho}{\rho_s} |_{z=L_u} - C_L \Phi_{L_l} \frac{\rho}{\rho_s} |_{z=L_l}$$

- **Conservation of mobile bed solid mass**

$$\frac{\partial}{\partial t} Z_b = - \frac{C_{Z_b} \Phi_{Z_b} \rho |_{z=Z_b}}{(1-p)}$$

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# Closure Equations

- **Bedload layer dynamics (Ferreira, 2005)**

$$\frac{h_2}{d_s} = m_1 + m_2 \theta \quad U_2 = U_1 \left( \frac{h_2}{h_1} \right)^{1/6}$$

- **Flow resistance**

$$\tau_{b_i} = C_f \rho \|\vec{u}\| u_i \quad C_f = \frac{gh^{1/3}}{K_s^2} \quad C_f = \frac{\|\vec{u}\| d_s}{h\omega_s}$$

$$\tau_i = \tau_y + \mu \frac{\partial u_i}{\partial z} + \rho d_s^2 c_f \left( \frac{\partial u_i}{\partial z} \right)$$

$$T_{ij} = \rho \nu_T \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$$

- **Bed morphology**

$$\frac{\partial Z_b}{\partial t} = \frac{q_s - q_s^*}{\Lambda} (1 - p)^{-1}$$

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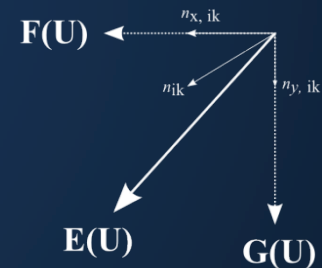
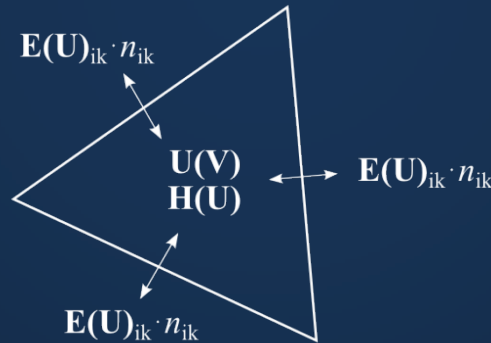
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# Discretization Scheme

- Finite Volume Method

$$\partial_t \mathbf{U}(\mathbf{V}) + \partial_x \mathbf{F}(\mathbf{U}) + \partial_y \mathbf{G}(\mathbf{U}) = \mathbf{H}(\mathbf{U})$$

$$\partial_t \int_{\Omega_i} \mathbf{U}(\mathbf{V}) dS + \oint_{\Gamma_i} \mathbf{E}(\mathbf{U}) \cdot \mathbf{n} dl = \int_{\Omega_i} \mathbf{H}(\mathbf{U}) dS \quad \mathbf{E} \cdot \mathbf{n} = \mathbf{F} n_x + \mathbf{G} n_y$$



$$\partial_t A_i \langle \mathbf{U}_i \rangle + \sum_{k=1}^N L_k \langle \mathbf{E} \cdot \mathbf{n} \rangle_{ik} = A_i \langle \mathbf{H}_i \rangle$$